

Phase shift ring-down spectroscopy in optical wave guides

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CRD user meeting, Cork, Ireland
Sept 18th-19th, 2006

Outline

1. Fibre-loop ring-down spectroscopy:

An absorption spectroscopic technique for very small samples

2. Fibre-cavity ring-down spectroscopy:

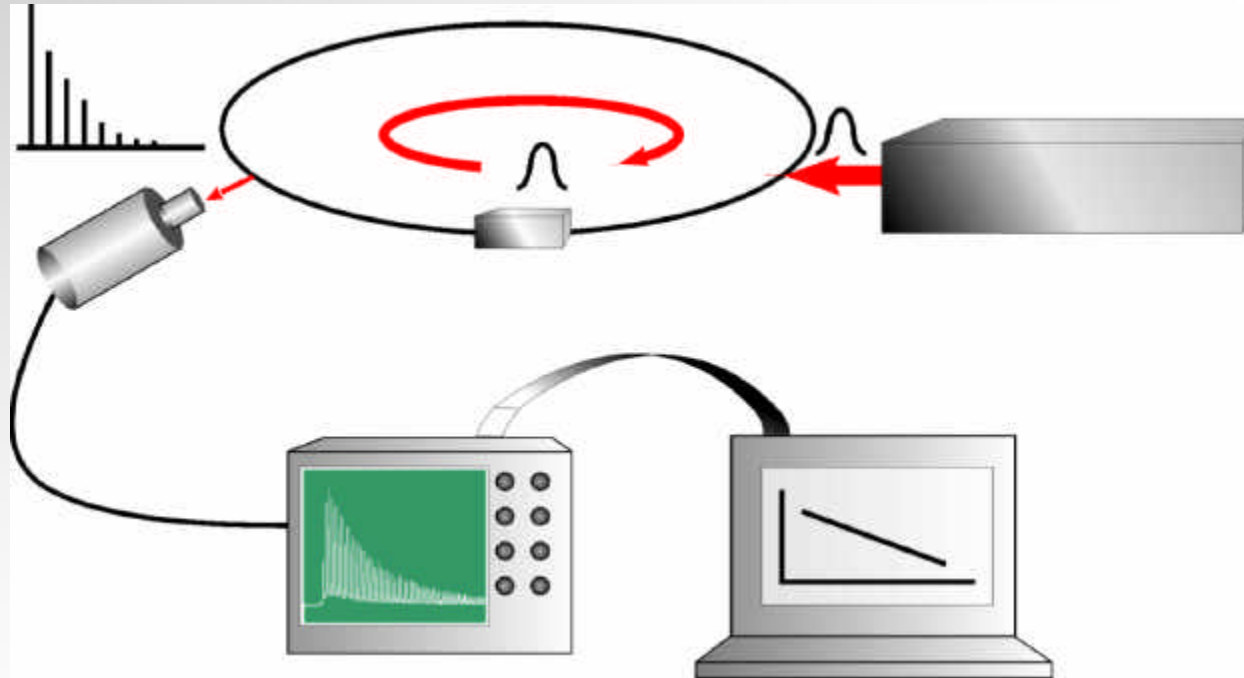
How to extract two independent (and short!) decay constants using phase-shift ring-down

3. Ring-down spectroscopy on microsphere resonators:

Measurements of absorption and refractive index

Chemical detection with telecom devices

Fibre-Loop Ring-Down Spectroscopy

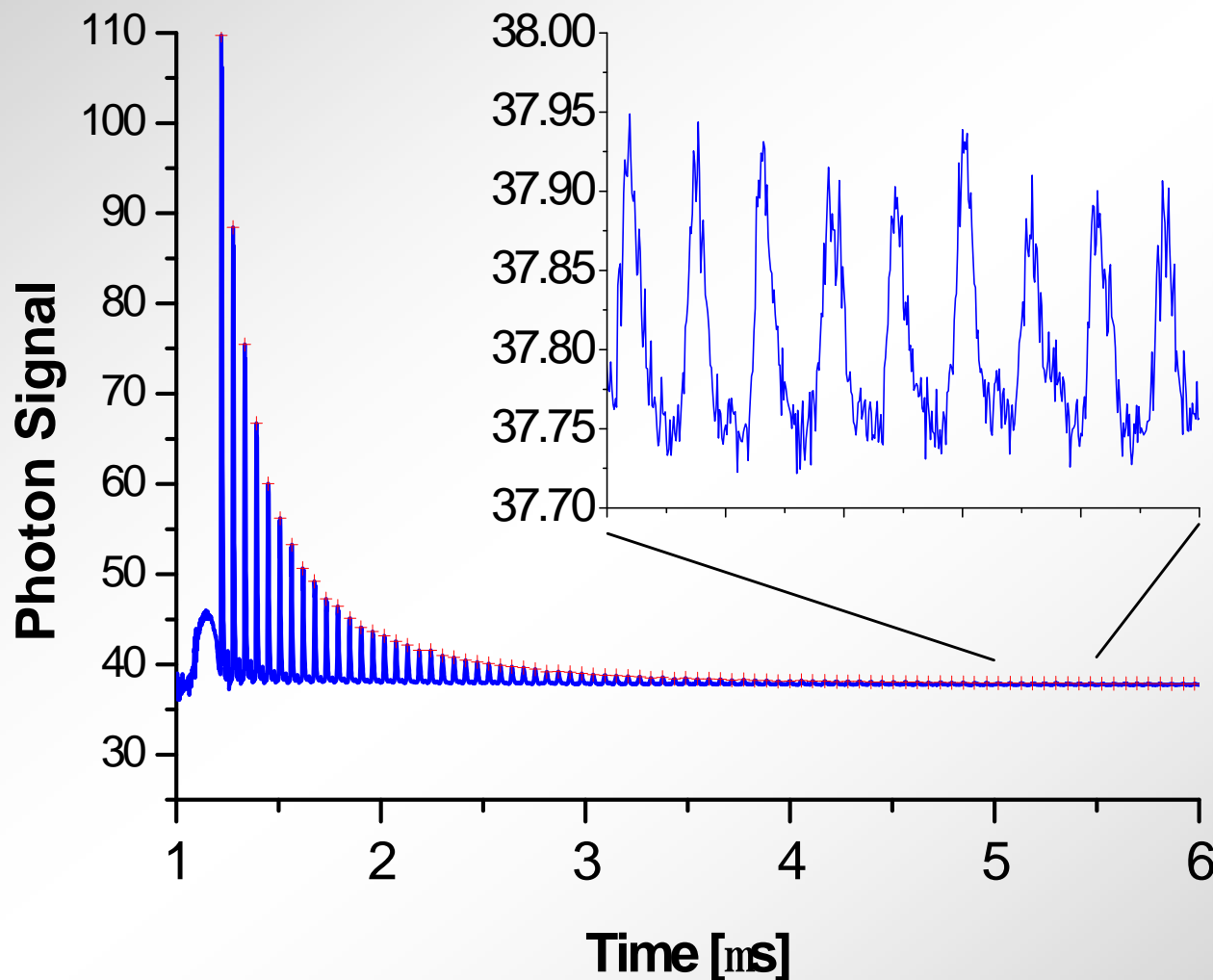
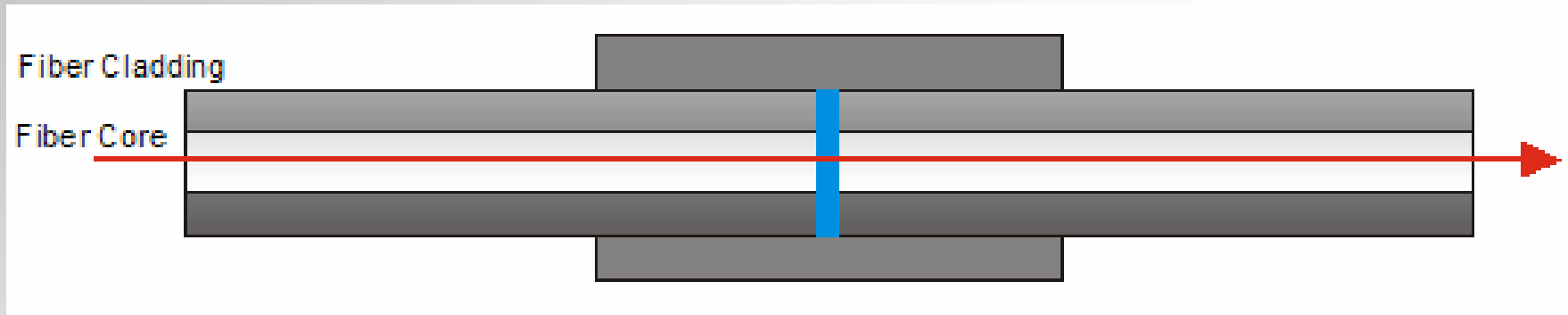


Cavity[®] fibre loop
Mirrors[®] splice

- FLRDS increases the effective absorption length by a factor of 100
- Ring-down time, τ , is independent of the pulse-to-pulse fluctuations.

G. Stewart, K. Atherton, H. Yu, B. Culshaw Meas. Sci. Technol. 12, **2001**, 843–849
Brown, R. S.; Kozin, I.; Tong, Z.; Oleschuk, R. D.; Loock, H.-P. *J. Chem. Phys.* **2002**, 117 (23), 10444-10447.
Tarsa, P. B.; Rabinowitz, P.; Lehmann, K. K. *Chem. Phys. Lett.* **2004**, 383 (3, 4), 297-303.

Ring-down trace for a 12 m fibre loop



Ring-down time

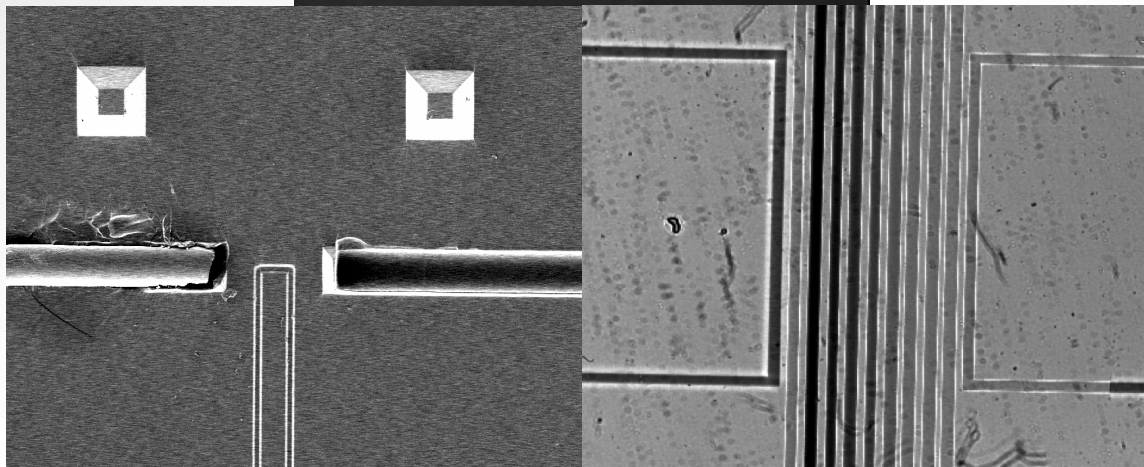
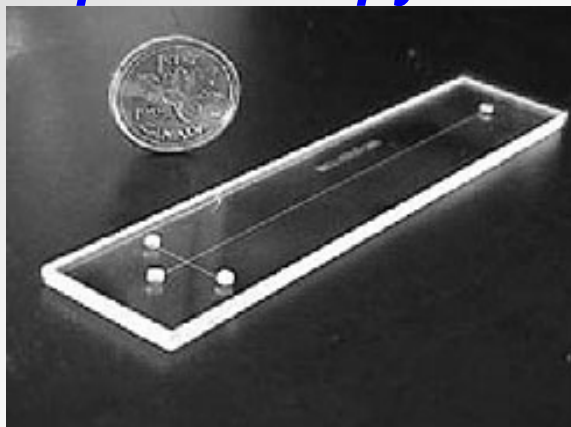
$$t = \frac{L}{c_0 (aL - \ln T_{splice})}$$

here:

$$\tau_1 = 600 \text{ ns}$$

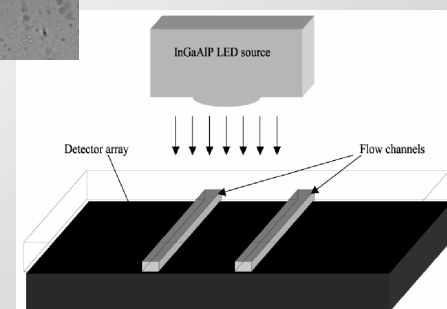
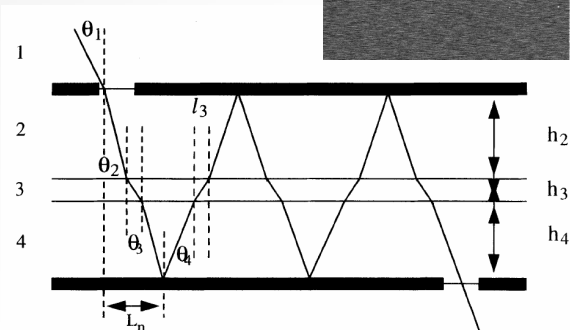
$$\tau_2 = 120 \text{ ns}$$

Absorption spectroscopy in microfluidics



Harrison, U.Alberta

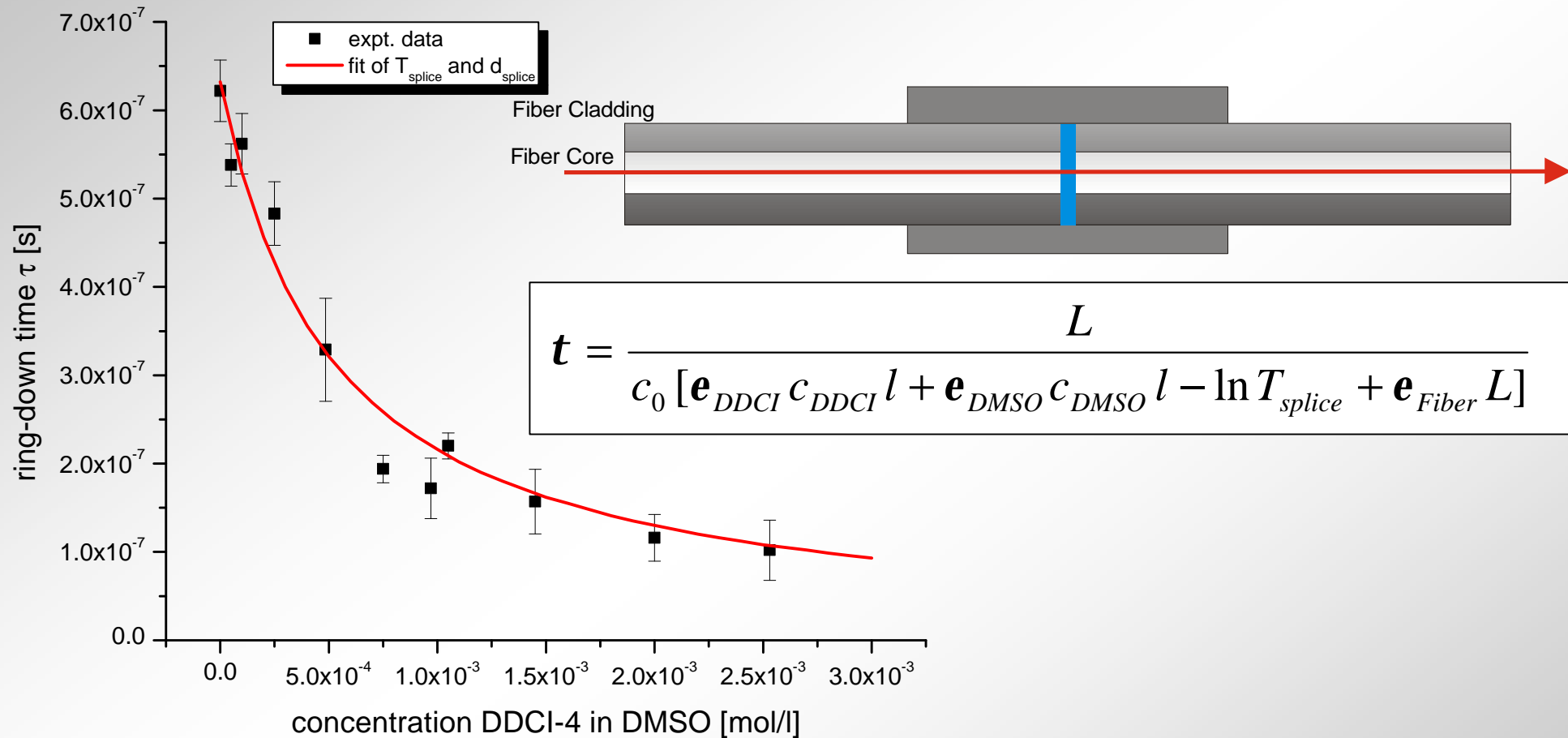
Adams, Caltech



Salimi-Moosavi,H.; Jiang,Y.T.; Lester,L.; McKinnon,G.; Harrison,D.J."A multireflection cell for enhanced absorbance detection in microchip-based capillary electrophoresis devices", Electrophoresis 21, 7(2000)

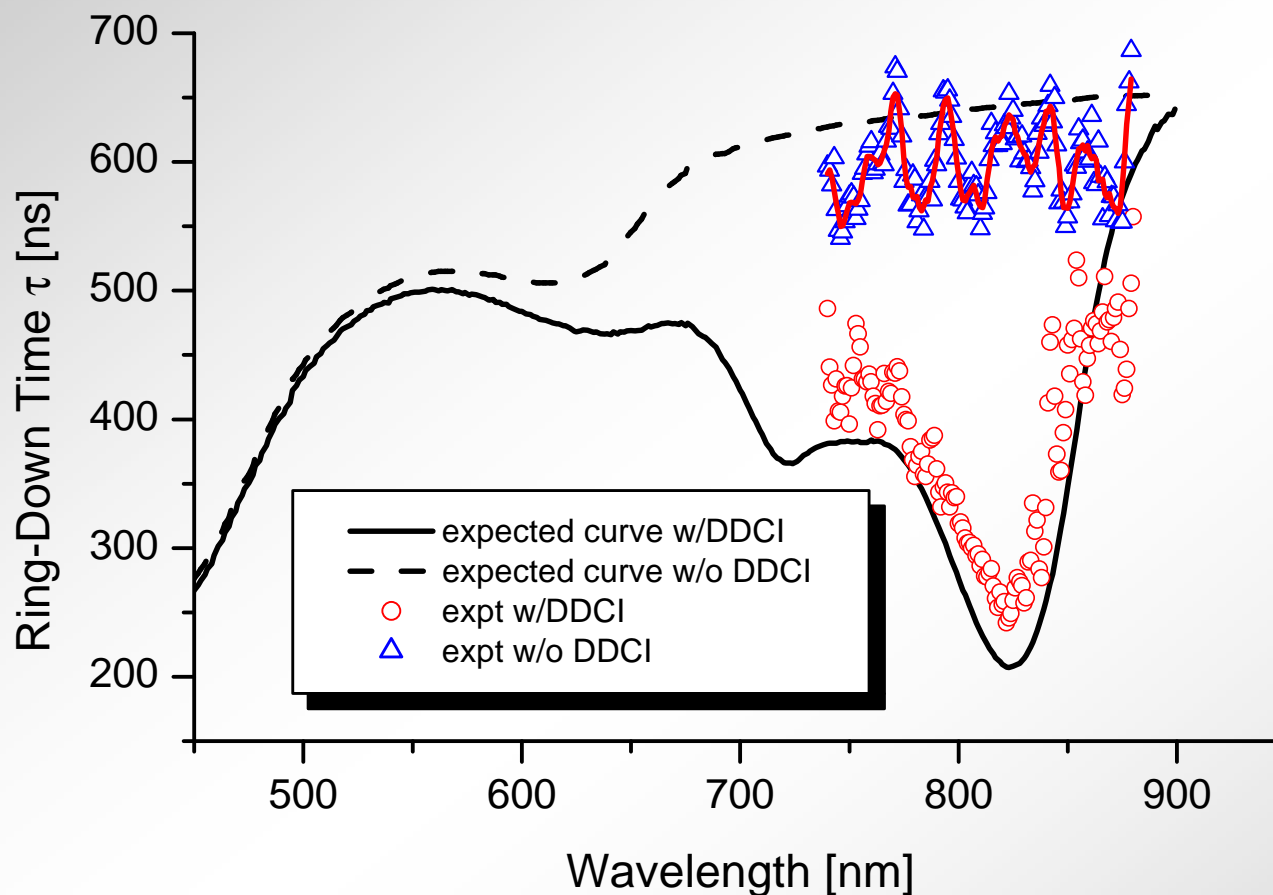
Adams,M.L.; Enzelberger,M.; Quake,S.; Scherer,A. "Microfluidic integration on detector arrays for absorption and fluorescence micro-spectrometers", Sensors and Actuators A-Physical 104,1 (2003)

Concentration dependence of τ (DDCI-4 in DMSO)



- Path length: $l = 3.8 \mu\text{m}$
- Volume sampled: 7 pL
- Detection limit: 1.4×10^{-15} mol of DDCI-4

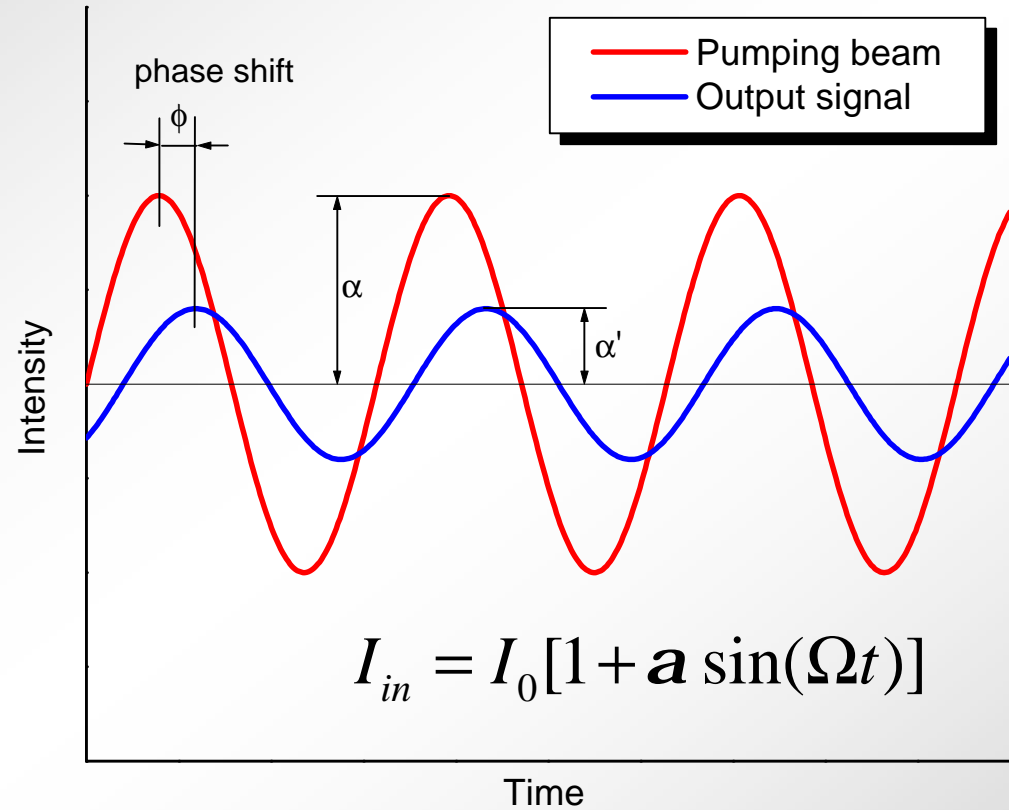
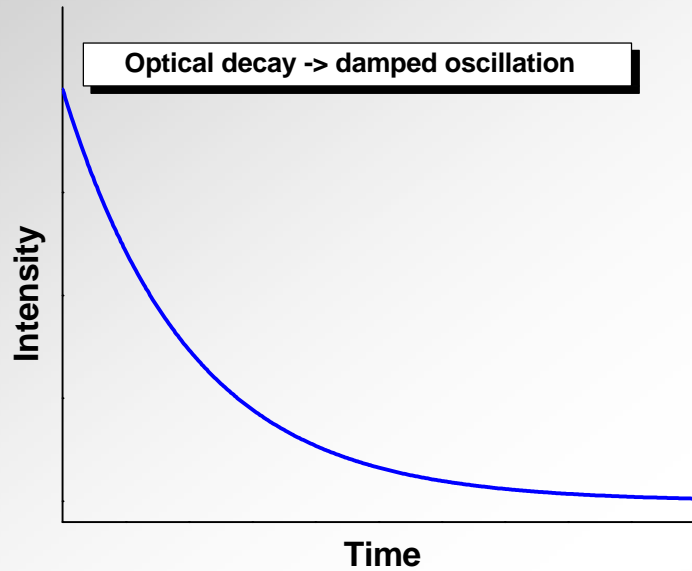
Absorption Spectrum of 7 pL of 1mMol DDCI-4



- Spectrum of 7pL of 1mM DDCI-4 in DMSO
- Assumes same 3.8 μm path length as before
- Fibre absorption increases dramatically <550nm

Stephen Brown, Igor Kozin, Zhaoguo Tong, Richard Oleschuk, and Hans-Peter Loock,
"Fiber loop ring down spectroscopy", **J. Chem. Phys.**, 11,23, (2002) 10444.

Phase-Shift Decay Measurement

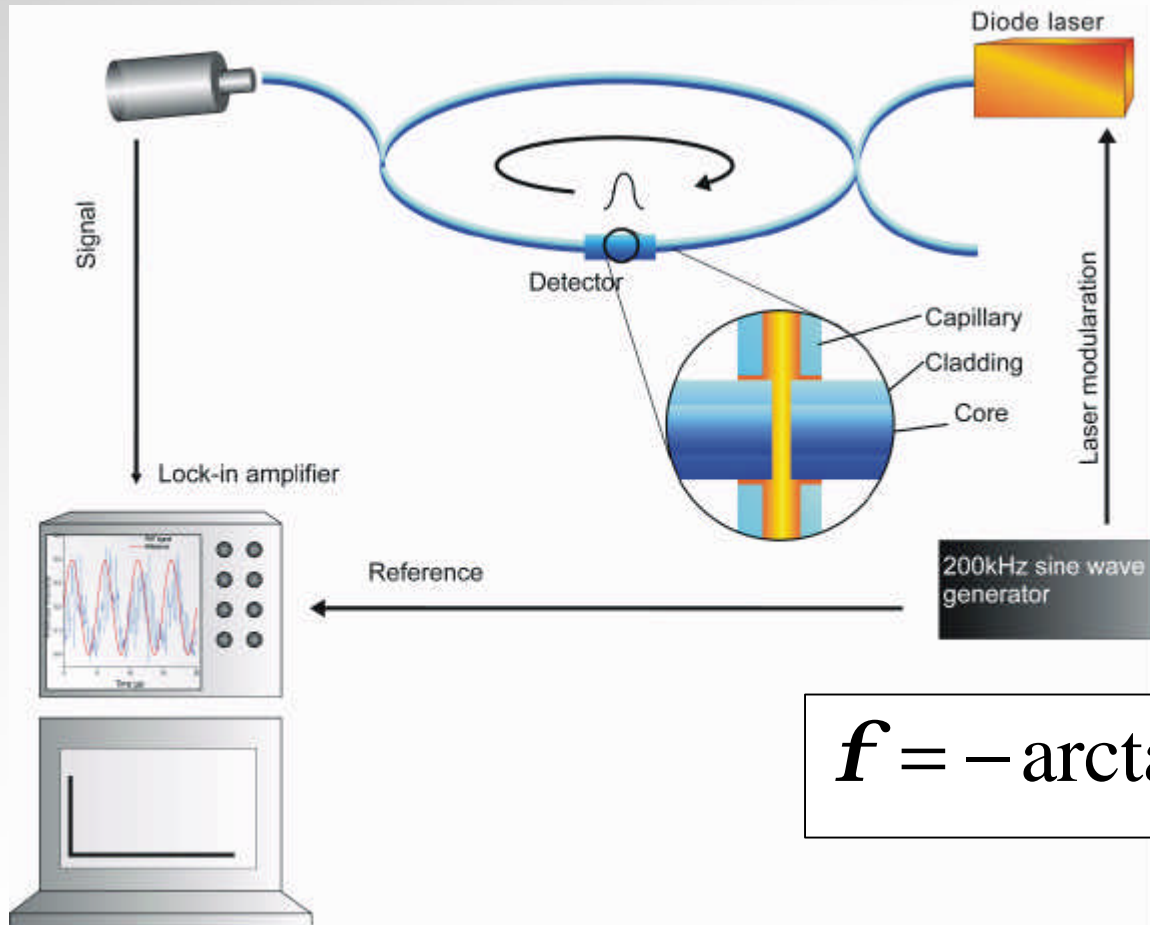


phase shift $f = -\arctan(\Omega t)$

reduced modulation depth

$$a' = \frac{a}{\sqrt{1 + \Omega^2 t^2}}$$

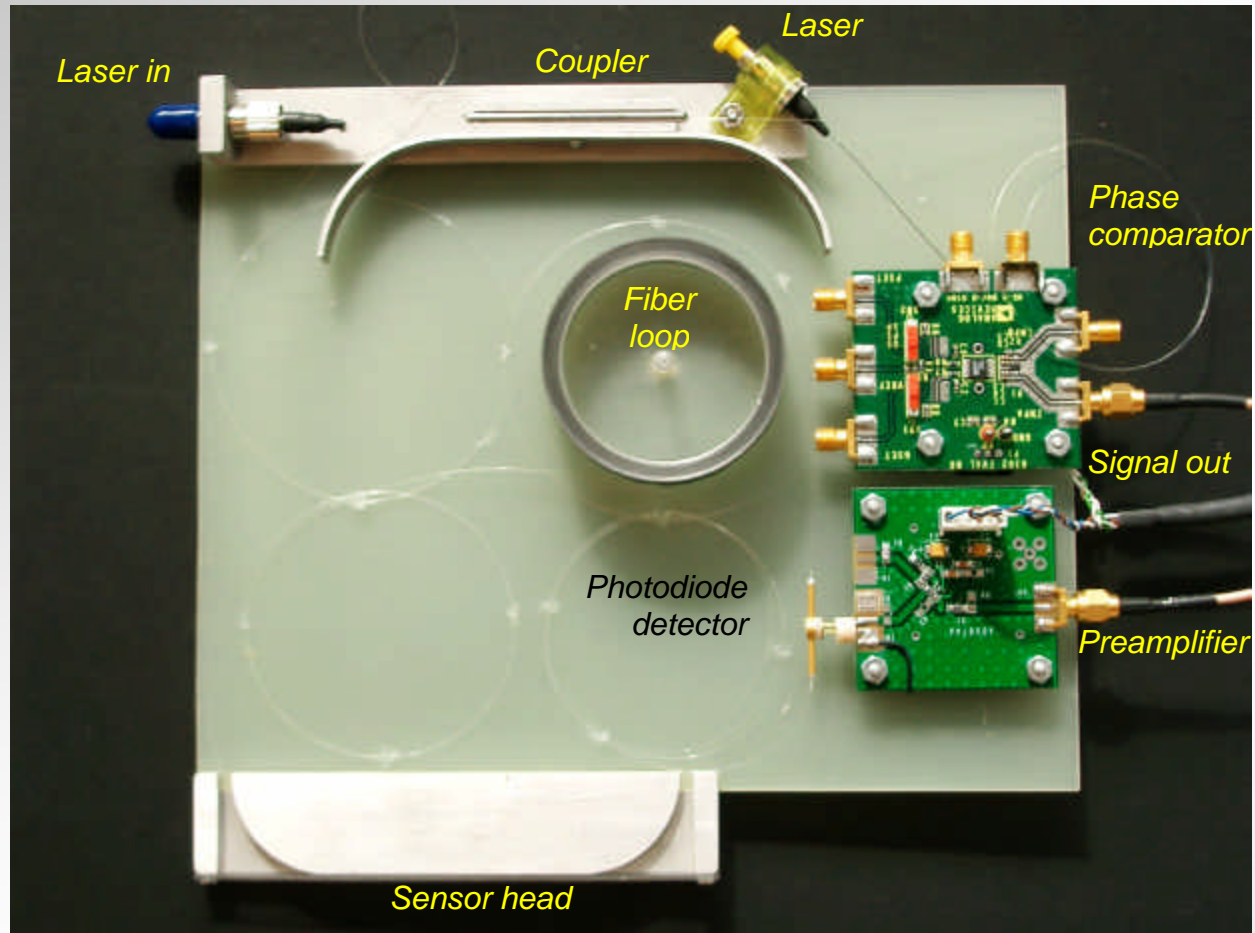
Phase-Shift FLRDS Setup



$$f = -\arctan(\Omega t)$$

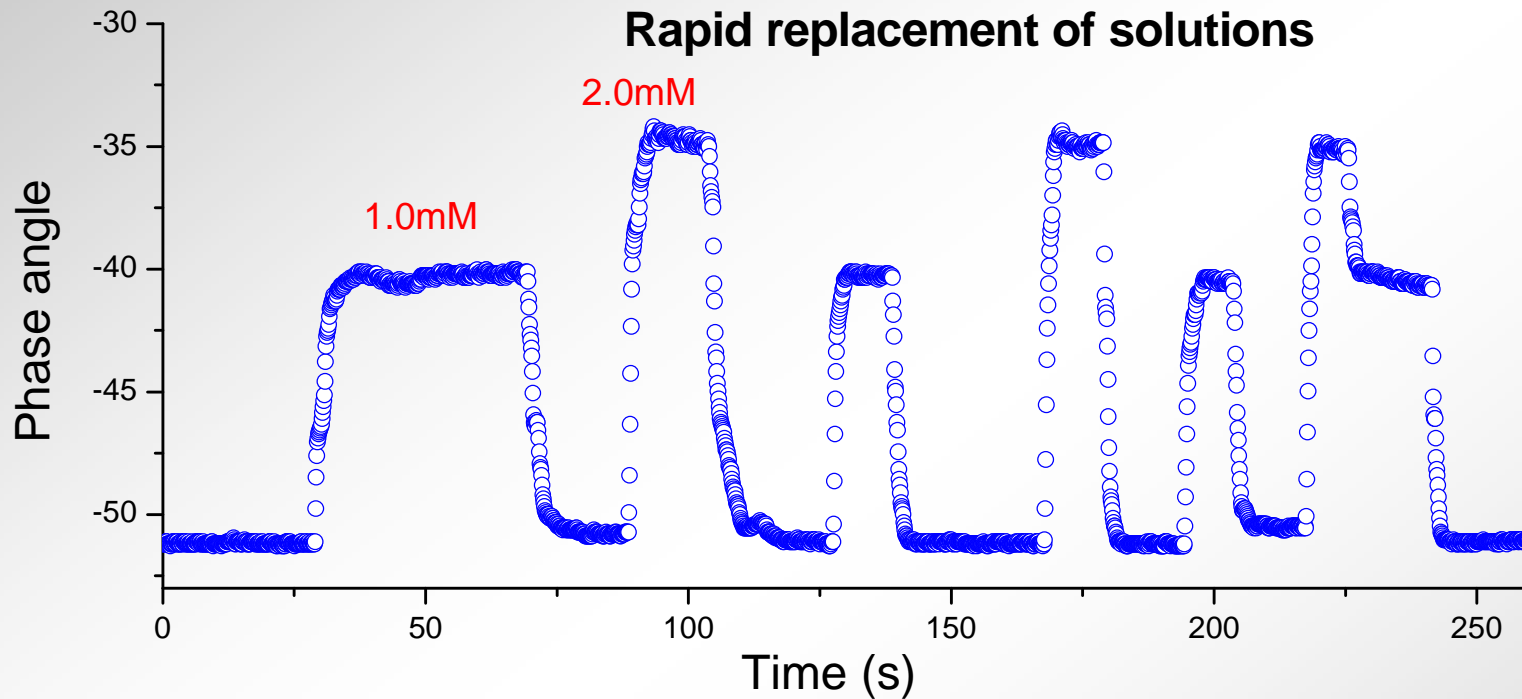
- Modulation frequency is about $\Omega/2\pi = 100$ kHz
- Transient signal is averaged by lock-in amplifier in 1 - 1000ms
- Laser Diode fixed $\lambda = 810$ nm

Phase-Shift FLRDS Setup



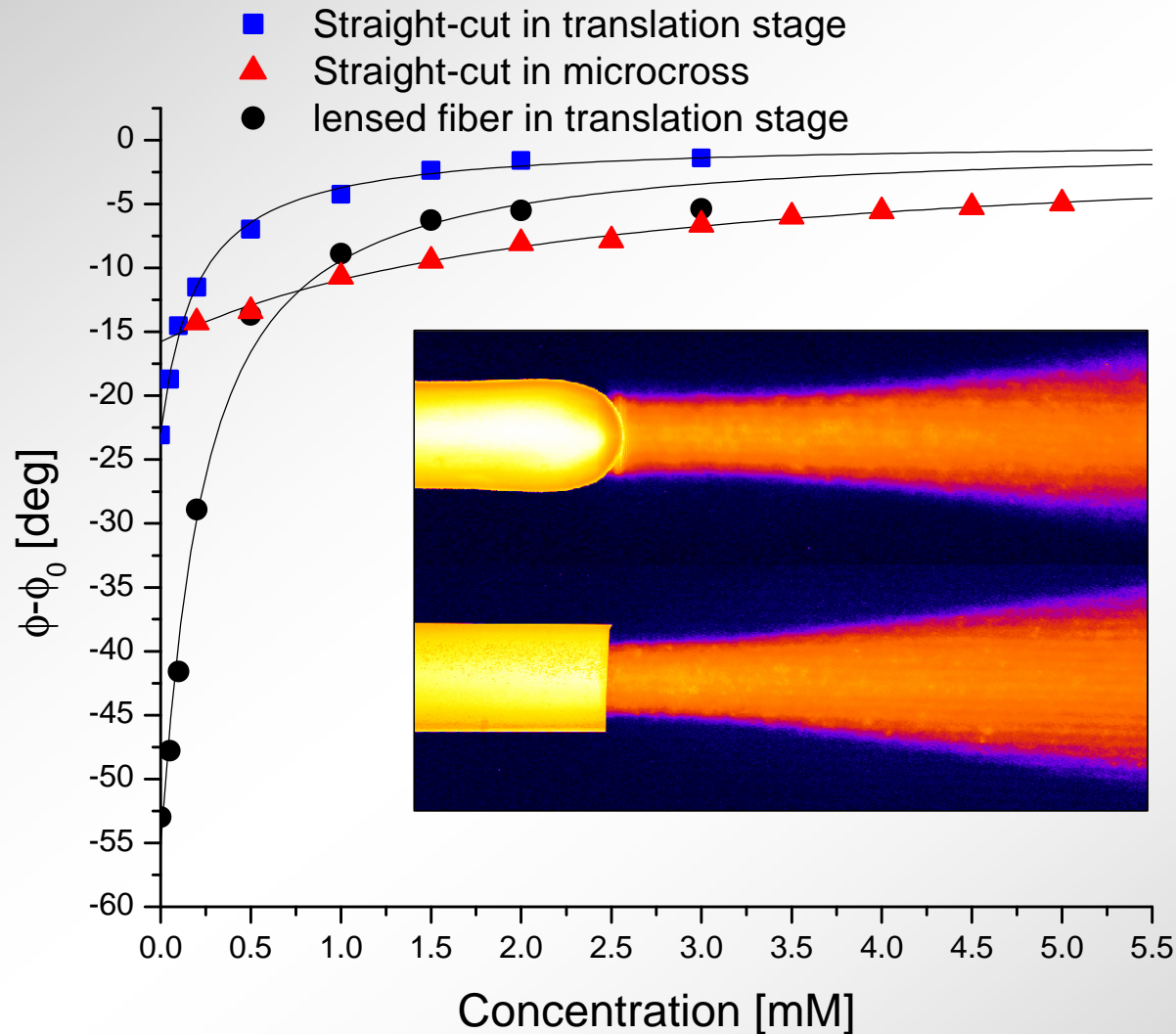
- custom-built circuitry capable of measuring phase shifts $\Delta\phi < 1^\circ$.

Time Resolution



- Time resolution: $< 100\text{ms}$,
 - sufficient to detect transient absorption peak in microfluidic devices
- No exponential fit involved
 - real-time measurements

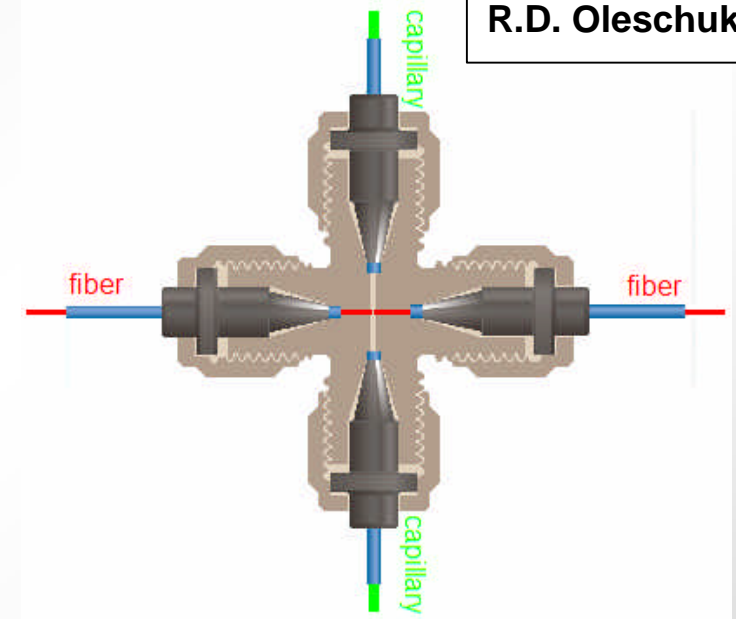
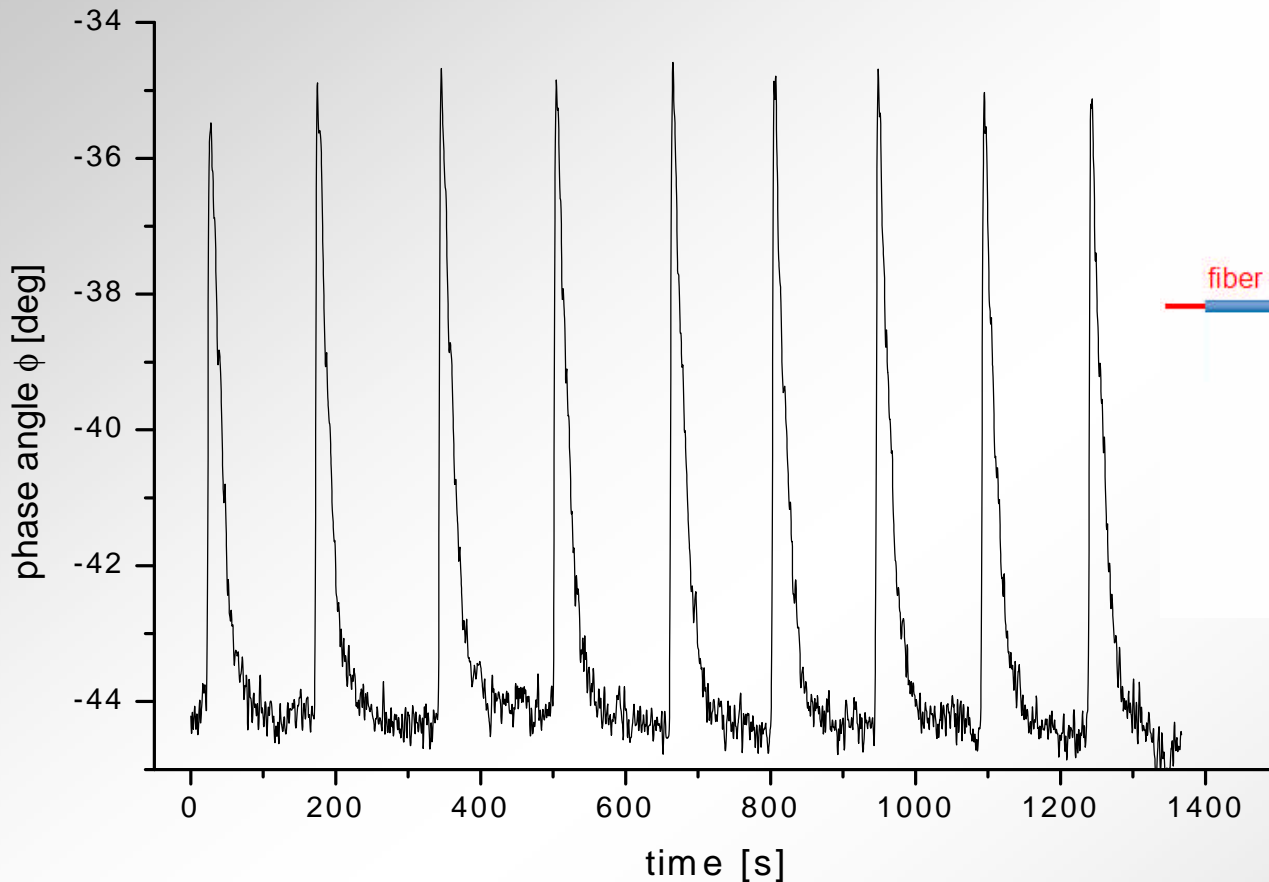
Lensed fibre ends dramatically increase sensitivity



- Lensed fibre ends in a have much lower transmission losses
→ lower detection limit of 70 attomoles in 280 pL

Application #1: Capillary Electrophoresis

Injections of 2.0 mM solution of ADS 832 ($C_{52}H_{56}ClN_3O_6S_3Na$)



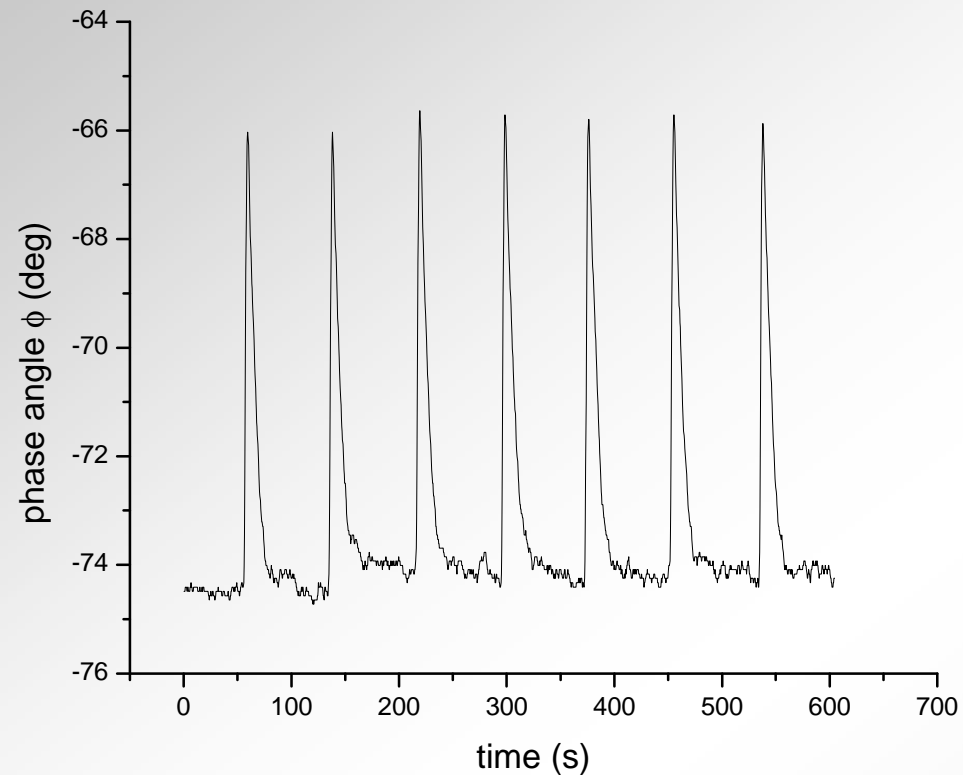
Runkai Li &
R.D. Oleschuk

- Reproducibility of peak areas better than 2%.
- Detection limit: 200 μ M
- Absorption path length of 140 μ m.
- Time resolution is about 100 - 200ms.

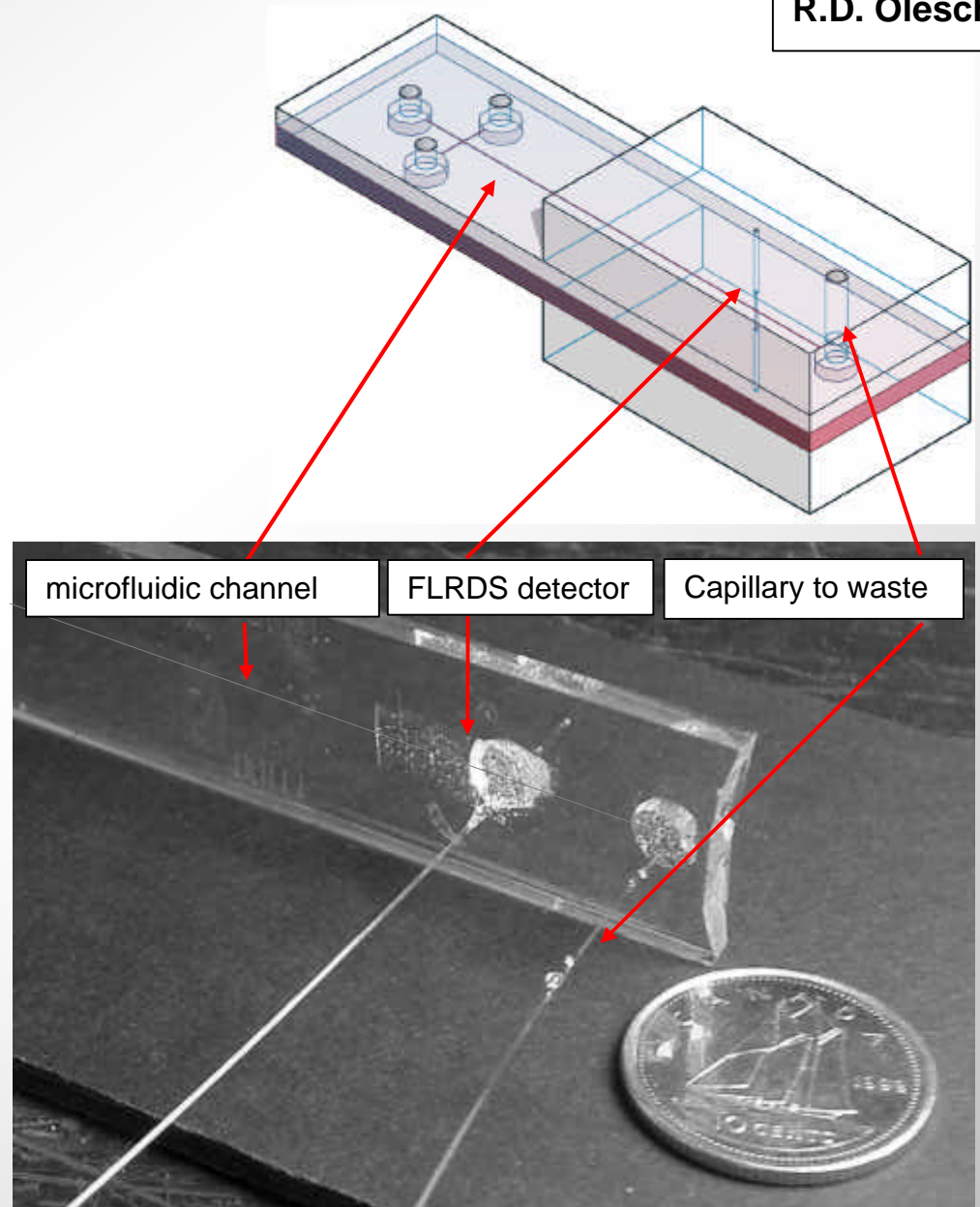
Application #2: Microfluidic Chip

Forced flow (multiple injections)

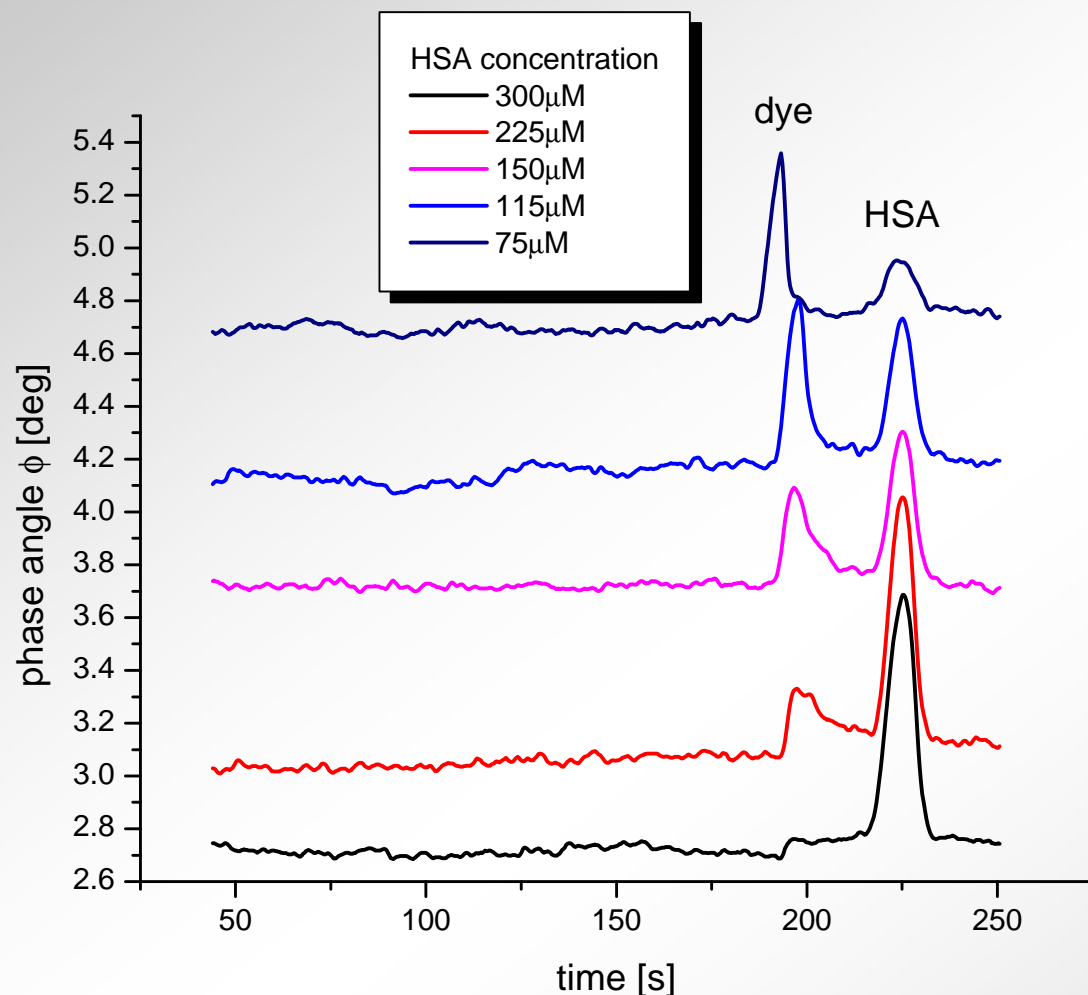
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R.D. Oleschuk



$c = 1.17 \text{ mM ADS805WS dye}$
Flow rate: $40 \mu\text{l/min}$
injection volume $2 \mu\text{l}$
sampling rate 3.33 Hz



Application #3: Capillary electrophoresis

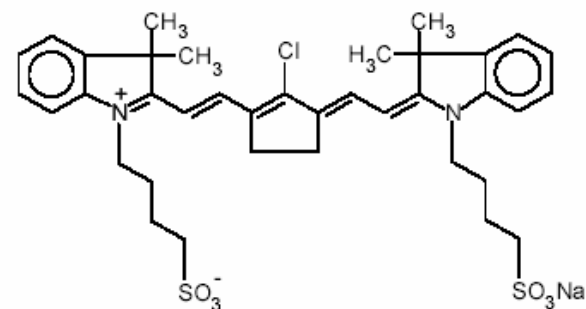


Dye concentration: 1.5 mM
 Capillary: 100/360 μm
 effective length 40 cm
 Separation voltage: 30 kV
 Injection: 5kV for 10s
 Buffer: 10 mM boric acid, pH=10.

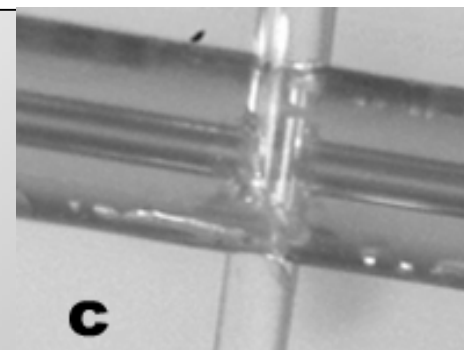
ADS 805

$\lambda_{\text{max}} = 807 \text{ nm}$

$\epsilon = 1.60 \times 10^5 \text{ L mol}^{-1} \text{ cm}^{-1}$

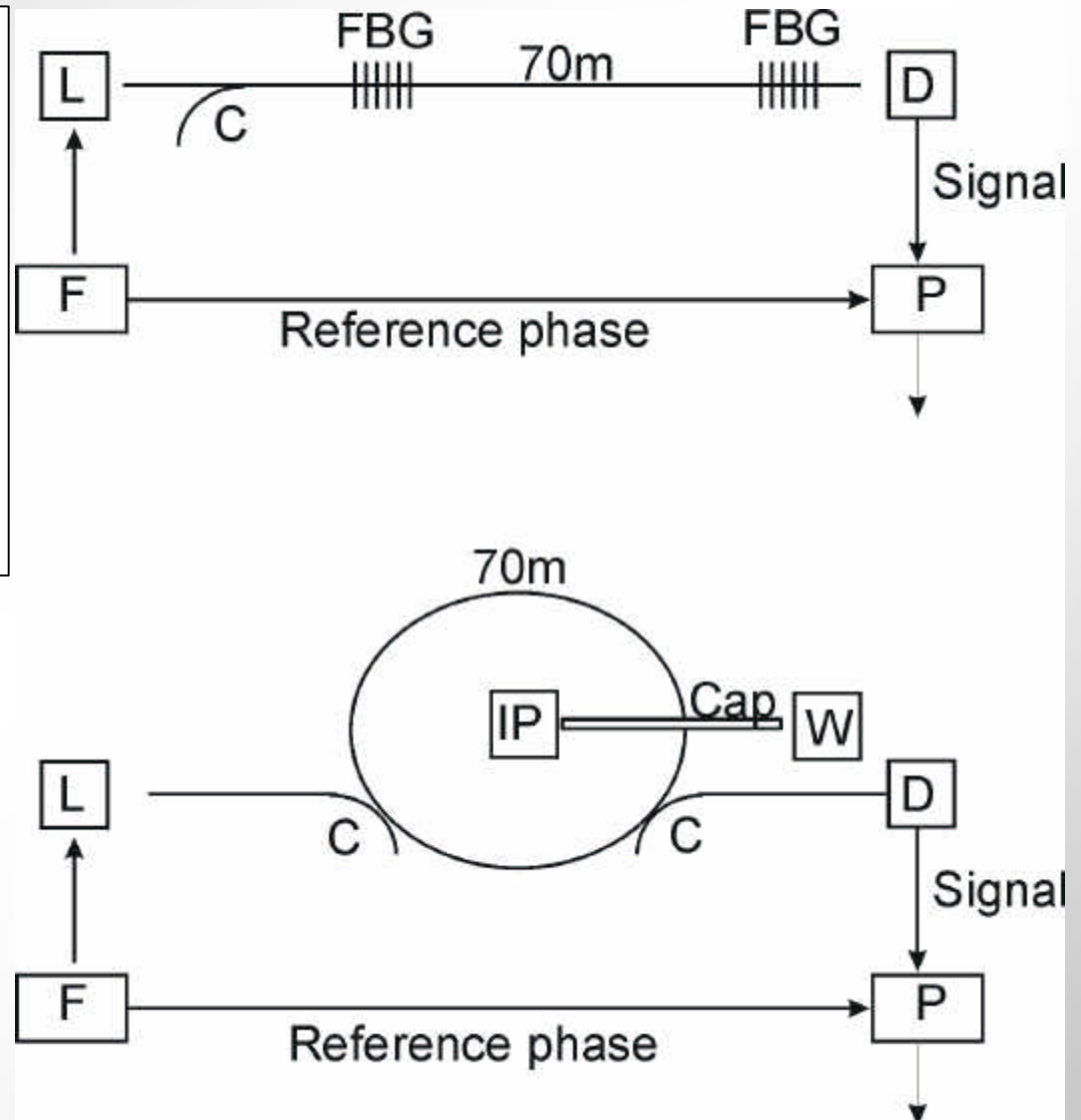


Separation of labeled Human Serum Albumin from free dye (labeling ratio ~6:1)



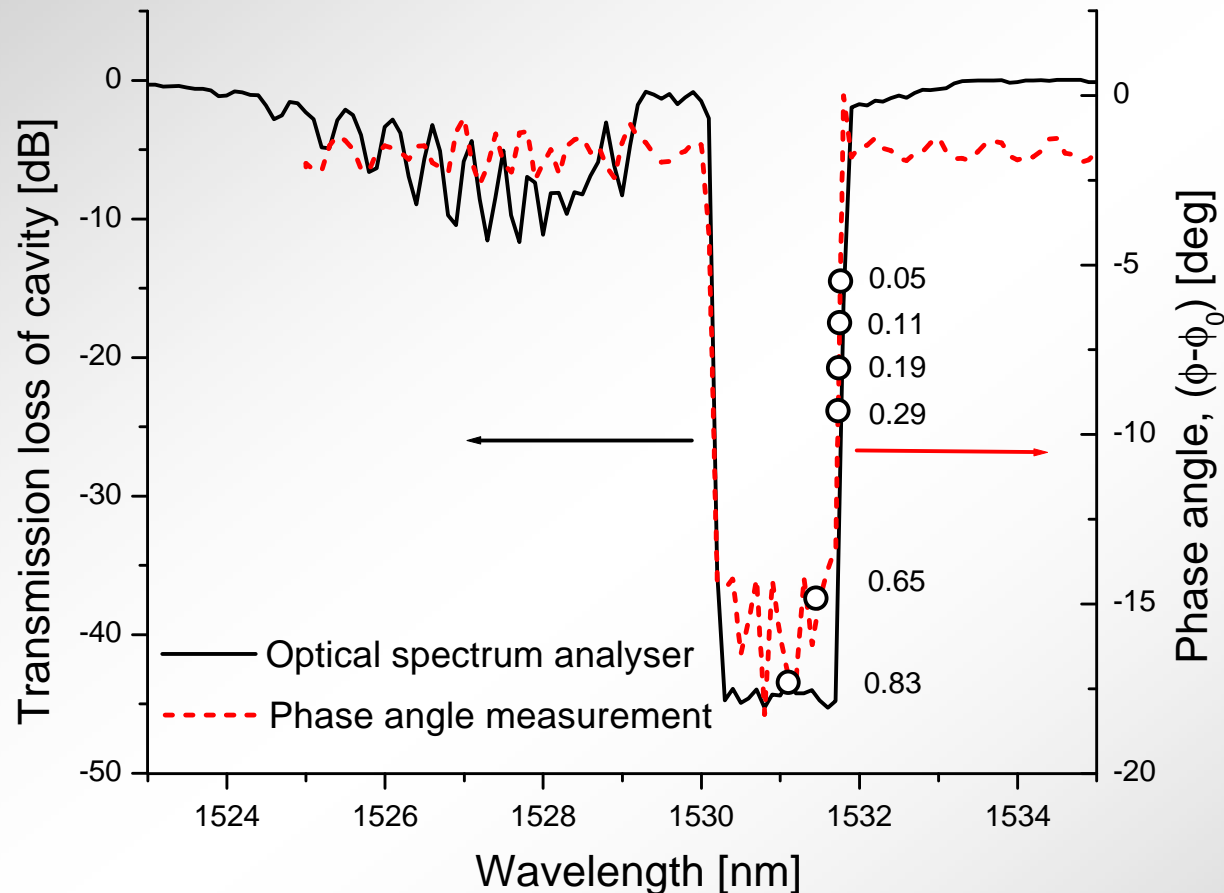
2. Fibre-cavity ring-down spectroscopy

(L) Laser
(F) Function generator
(D) photodetector
(C) [99:1] fibre-fibre couplers
(P) phase comparator
(cap) capillary
(IP) injector pump
(W) waste compartment



● Fibre-Bragg Grating (FBG): “mirror” for single mode fibre

Linear cavity transmission spectrum



- Two decay processes with constant decay times ($\tau_1 < 50$ ns, $\tau_2 = 1.2\mu\text{s}$)
- Contribution of these two processes is wavelength dependent

Digression

How to model biexponentials if only one observable: phase angle

Mathematical Model

For a multiexponential decay function the **impulse response function** can be expressed as

$$I(t) = \sum_i^n a_i \exp(-t / t_i) \quad (1)$$

With

$$g_i = \frac{a_i t_i}{\sum_i a_i t_i} \quad (2)$$

Eq 1 is a linear time-invariant causal expression and its **Laplace transform** is

$$L(I(t)) = \sum_i \frac{a_i t_i}{t_i s + 1} \quad (3)$$

where

$s = j\omega + \sigma$, with $j = \sqrt{-1}$,

$\sigma = 0$ for an undampened system,

and the angular frequency $\omega = 2\pi f$.

Collaborator:

Gianluca Gagliardi,
Istituto Nazionale di Ottica Applicata, Naples, IT

Peter J. Verveer, Anthony Squire, and Philippe I. H. Bastiaens,
“Global Analysis of Fluorescence Lifetime Imaging Microscopy Data”
Biophys.J. 78 (2000) 2127–2137

E. Gratton, D. M. Jameson, R.D. Hall, *Multifrequency Phase And Modulation Fluorometry* **Ann. Rev. Biophys. Bioeng.** 13 (1984) 105

E. Gratton, D. M. Jameson, *New Approach to Phase and Modulation Resolved Spectra* **Anal. Chem.**, 57 (1985) 1694-1697

Separation of real and imaginary parts leads to

$$\mathbf{L}(I(t)) = jN_w + D_w \quad (4)$$

With

$$N_w = -\sum_i \frac{wa_i t_i^2}{w^2 t_i^2 + 1}$$
$$D_w = \sum_i \frac{a_i t_i}{w^2 t_i^2 + 1} \quad (5)$$

The associated phase angle is

$$\tan \mathbf{f} = \frac{N_w}{D_w} \quad (6)$$

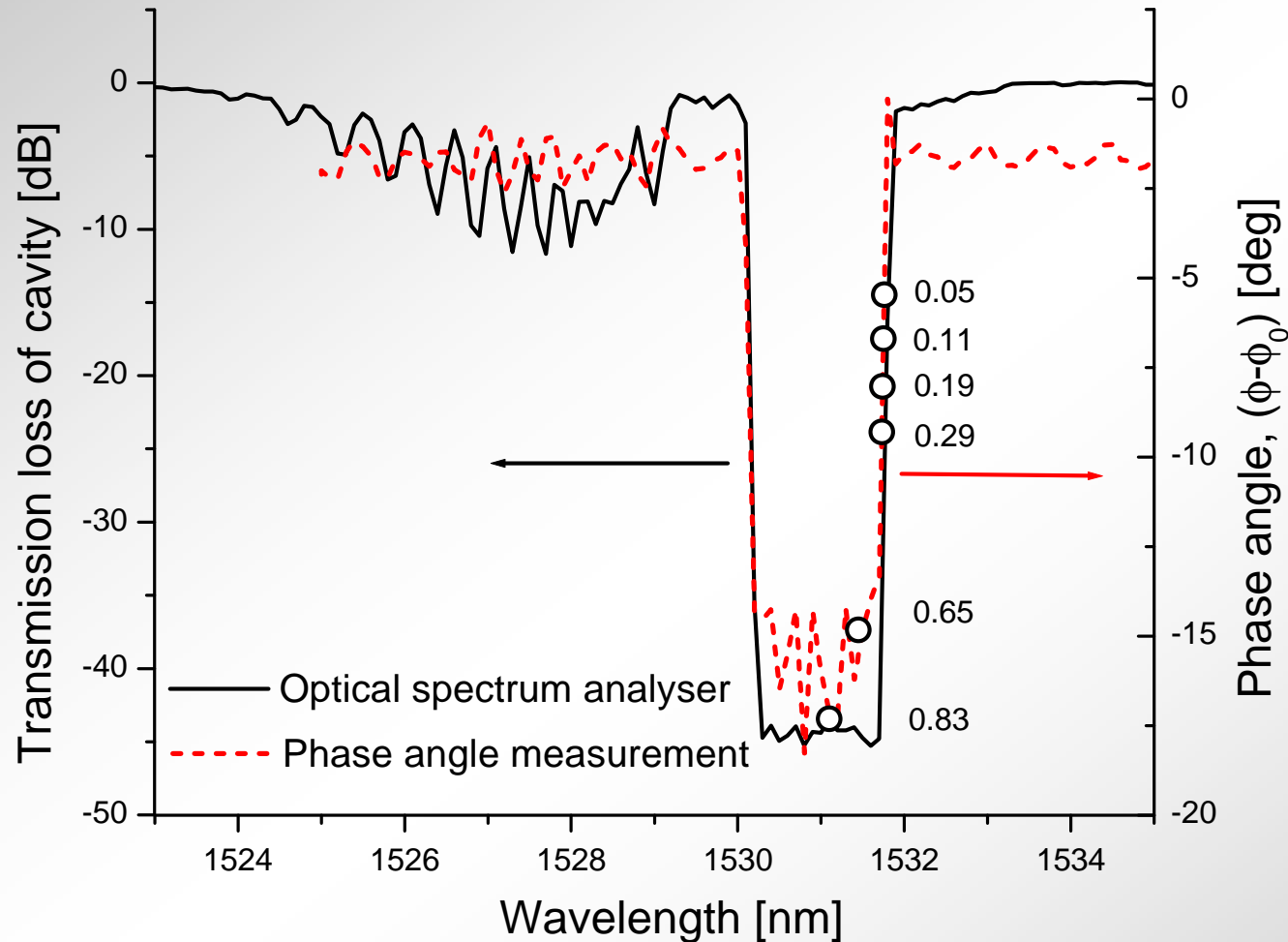
And the modulation depth is given by

$$M \sum_i a_i t_i = \sqrt{N_w^2 + D_w^2} \quad (7)$$

For a single-exponential decay

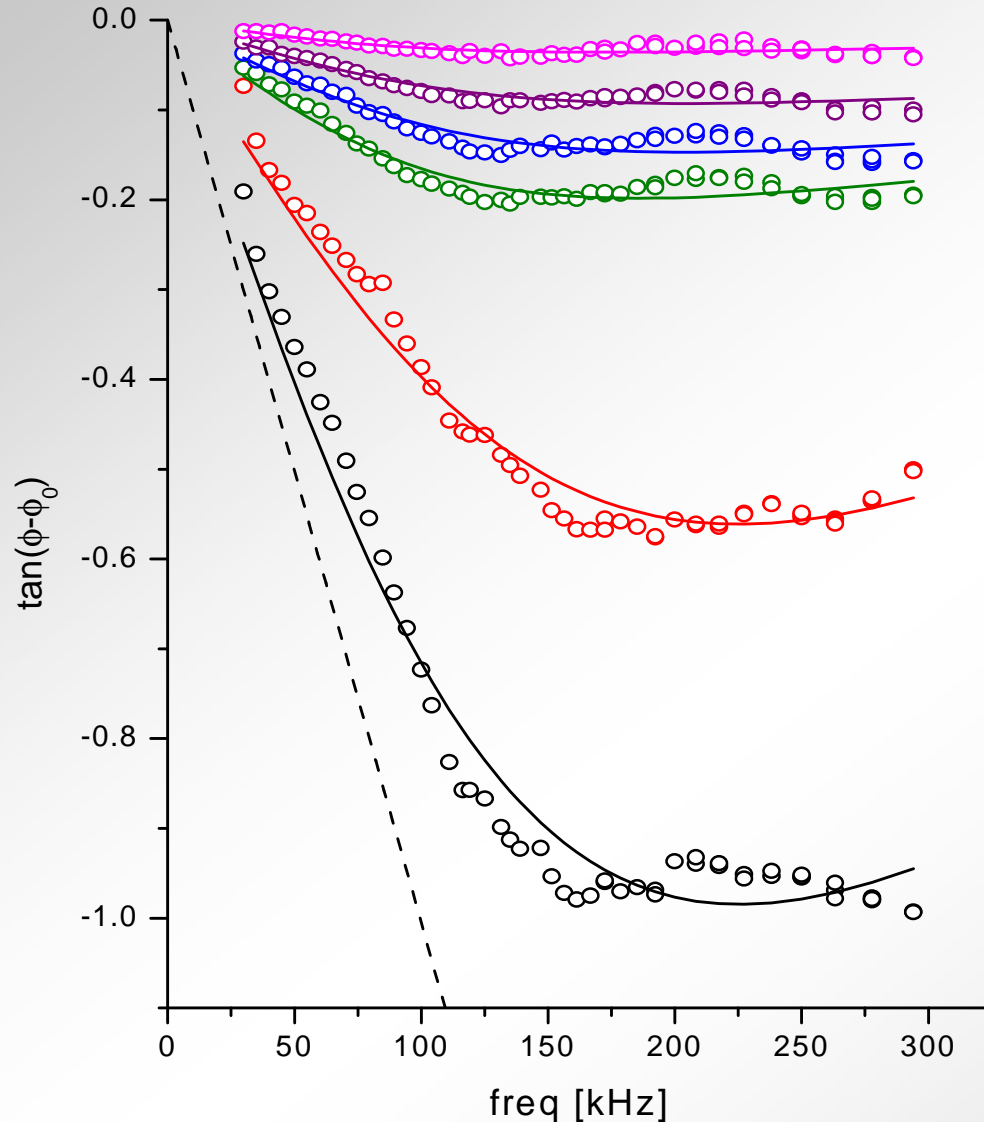
$$\tan \mathbf{f} = -wt$$
$$M = \frac{1}{\sqrt{1 + w^2 t^2}} \quad (8)$$

FBG cavity



- Light is either trapped in the cavity or transmitted ($\tau_1 > 1\mu\text{s}$ and $\tau_2 = 0\text{s}$)
- Fraction of trapped light changes near the edge of the cavity transmission spectrum

Example 1: FBG cavity

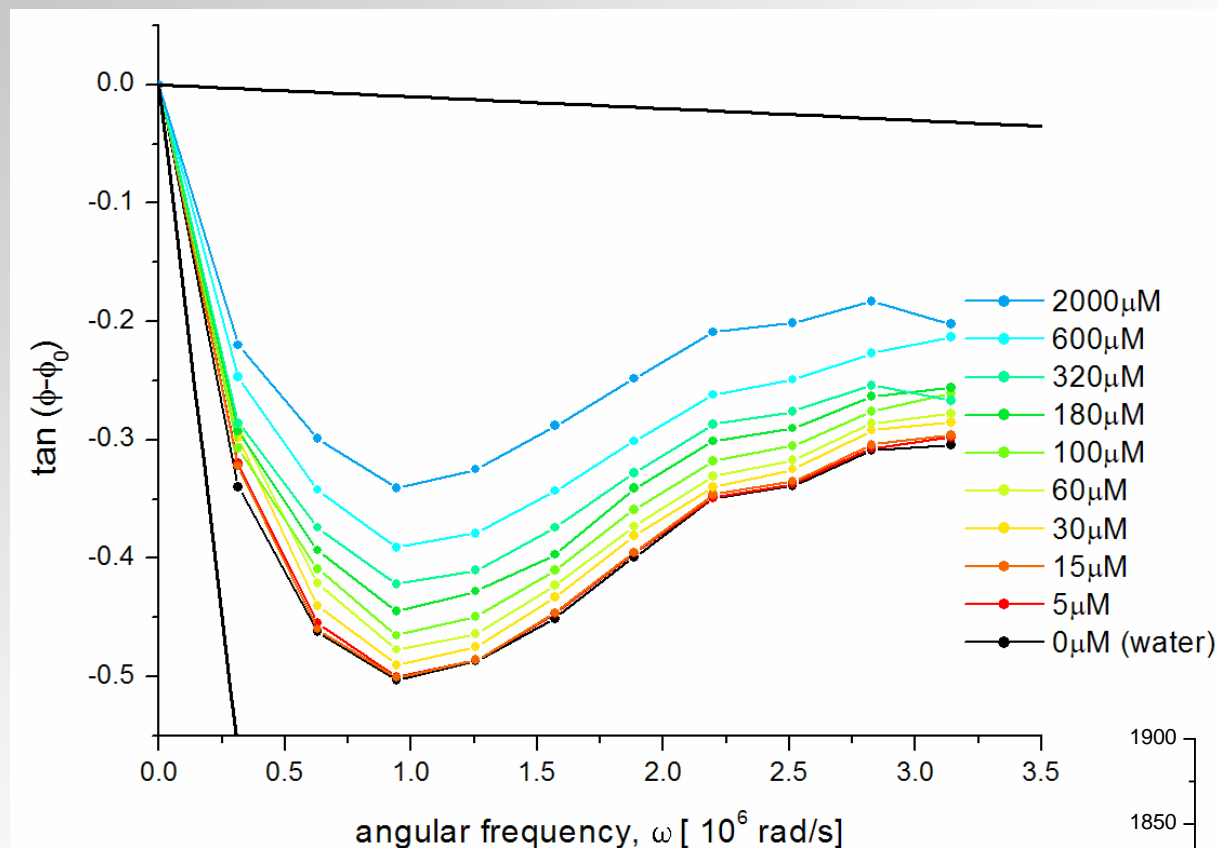
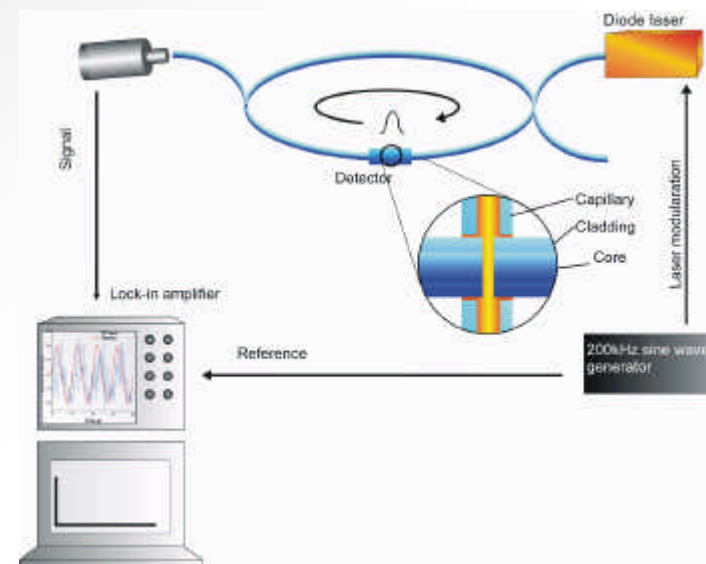


λ [nm]	τ_1 [μ s]	τ_2 [ns]	γ
1531.76	1.27(22)	8(5)	0.05
1531.75	1.22(14)	26(5)	0.11
1531.74	1.18(12)	34(9)	0.19
1531.73	1.18(12)	26(8)	0.29
1531.45	1.12(4)	0	0.65
1531.10	1.63(3)	0	0.83

$$\tan f = -\Omega t$$

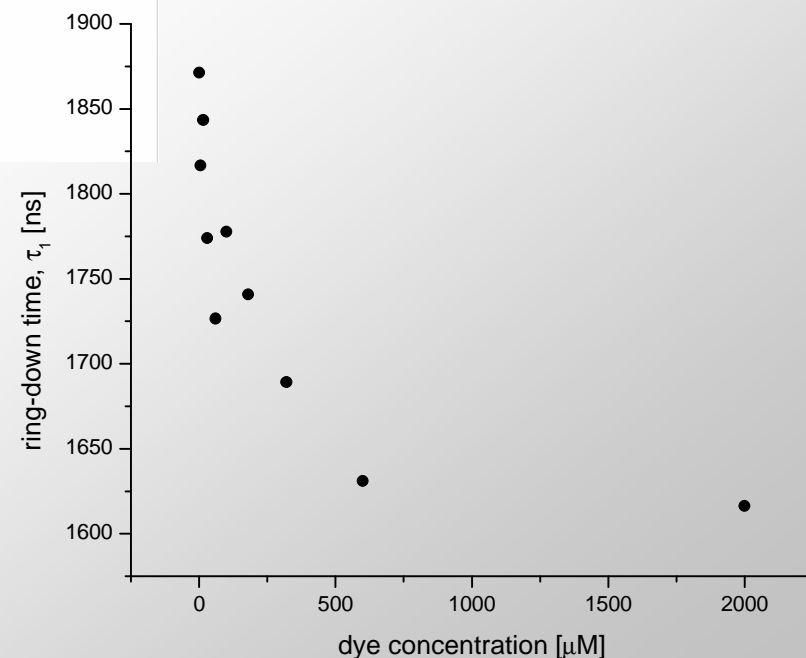
- Assuming a biexponential decay
- Agrees well with two fixed RDT's ($\tau_1 = 1.2\mu\text{s} - 1.6\mu\text{s}$; and $\tau_2 = 0\text{s}$)

Example 2: Fibre-loop ring-down detection

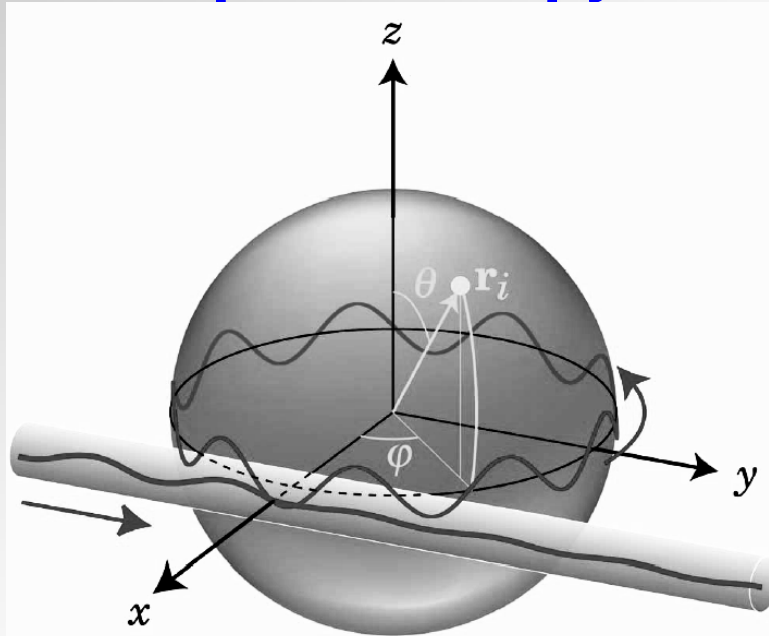


- Assuming a biexponential decay
- One fixed RDT's ($\tau_2 = 10\text{ns}$)
- An alternative way of correcting for ASE in diode laser CRD experiments

(see van Helden, Schram, Engeln, CPL 400 (2004) 320)



3. Ring-down spectroscopy on microsphere resonators



Collaborators:

Scott Yam, El. Engineering
James Fraser, Physics
Richard Oleschuk, Chemistry

- “Whispering Gallery modes” experience very low loss.
- Extremely high finesse cavity with Q-factor of 10^6 to 10^9
- Cavity length: here $L = \pi 300\mu\text{m} = 1\text{mm}$
 - short ring-down time
 - large free-spectral range

Is ring-down spectroscopy possible?

Ring-down time

$$t = \frac{L}{c_0 (aL - \ln T_{splice})}$$

$$\tan f = -\Omega t$$

Ring-down spectroscopy on microsphere resonators

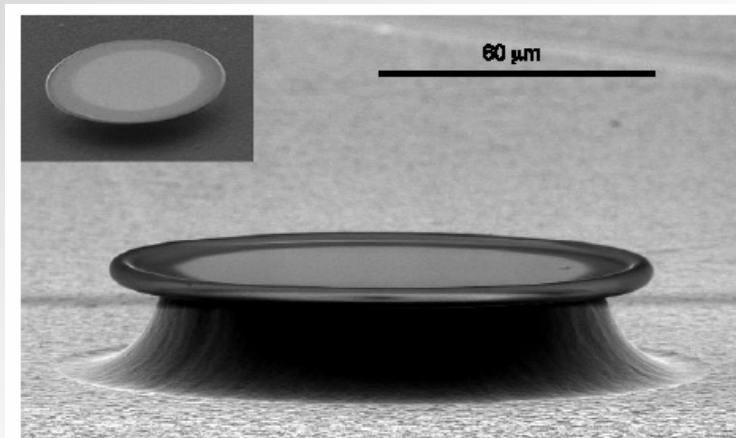


Figure 2 Scanning electron micrograph of a silica microdisk after selective reflow treatment with a CO₂ laser. The inset shows the microdisk prior to laser treatment. This toroidal microresonator had an intrinsic cavity Q of 1.00×10^8 .

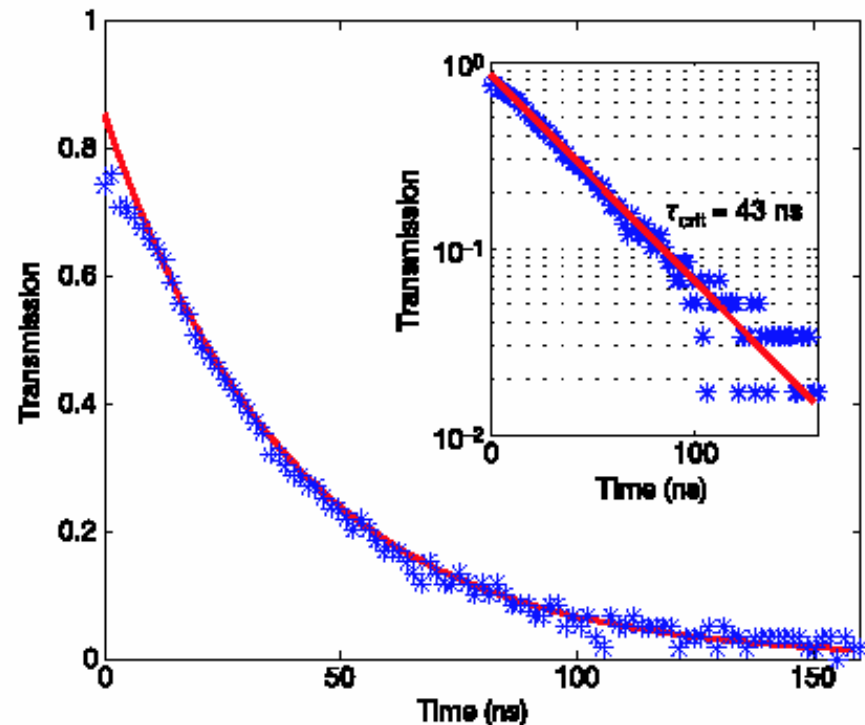


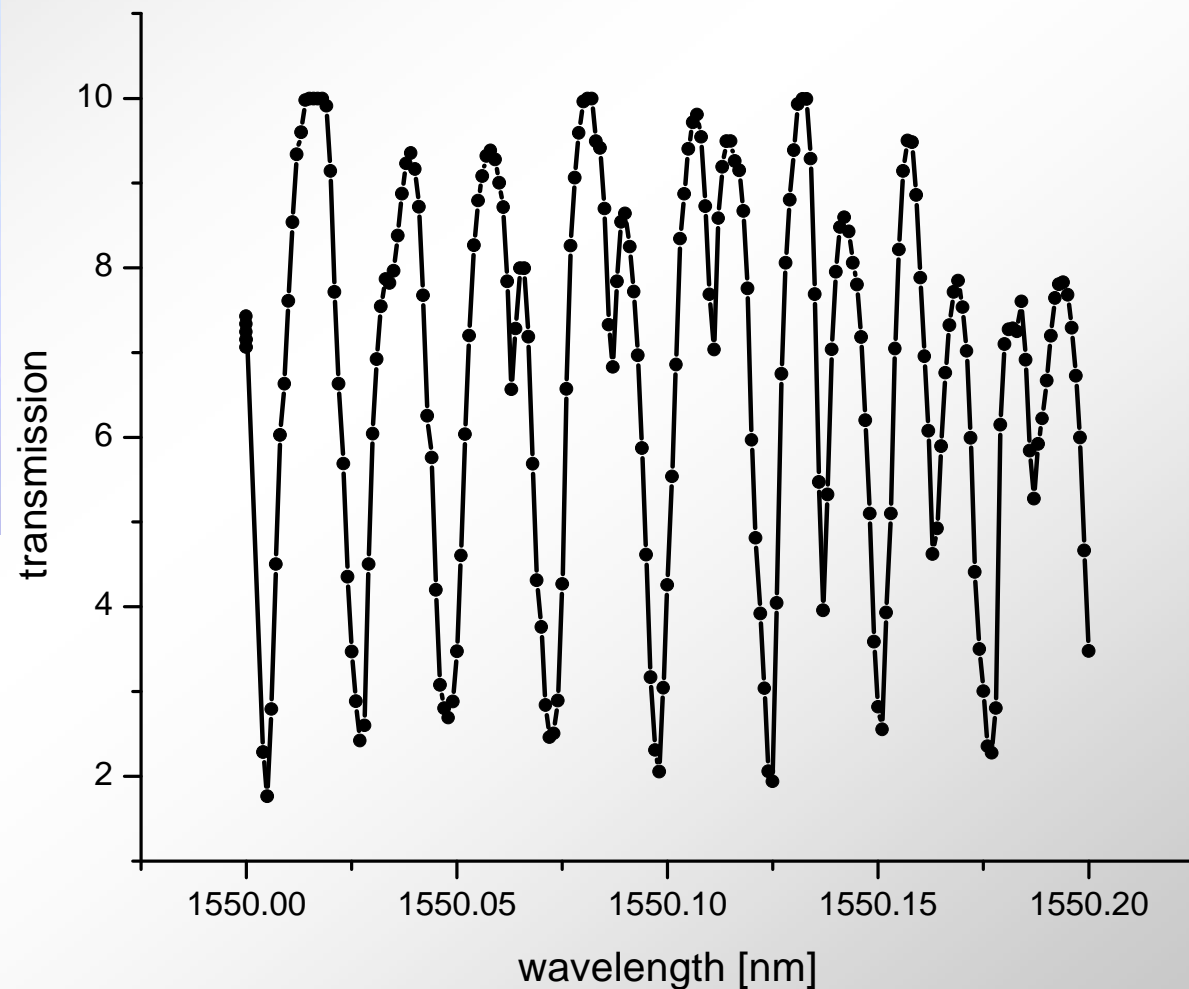
Figure 4 Ringdown measurement of a 90-μm-diameter toroid microcavity at the critical-coupling point. The measured lifetime of $\tau_{\text{crit}} = 43 \text{ ns}$ corresponds to an intrinsic quality factor of $Q = 1.25 \times 10^8$.

$$Q = 1.25 \cdot 10^8$$

Ultra-high-Q toroid microcavity on a chip

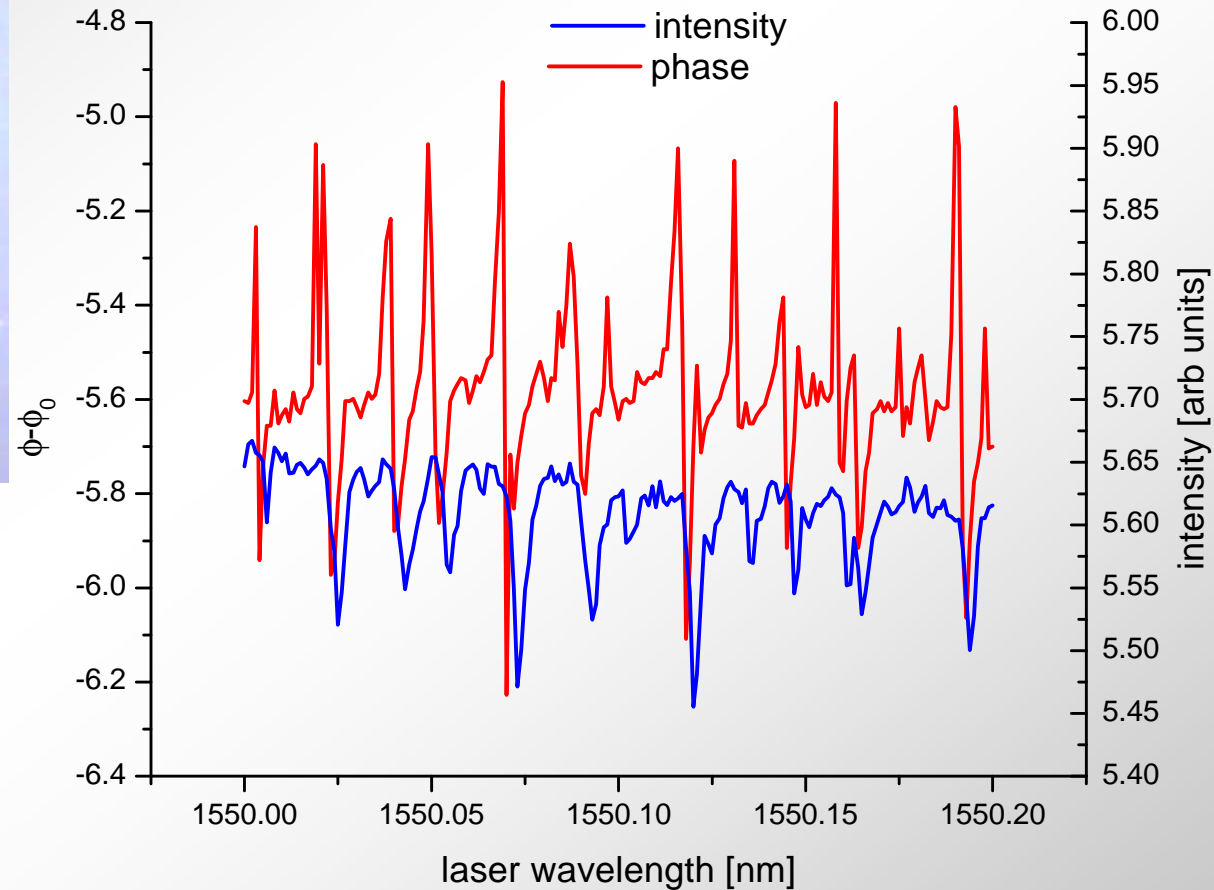
D. K. Armani, T. J. Kippenberg, S. M. Spillane & K. J. Vahala,
Nature, 421 (2003) 925

Ring-down spectroscopy on microsphere resonators



- Eroded fibre gives good coupling (very easy to break, though!)
- Tapered fibre just as good and more robust

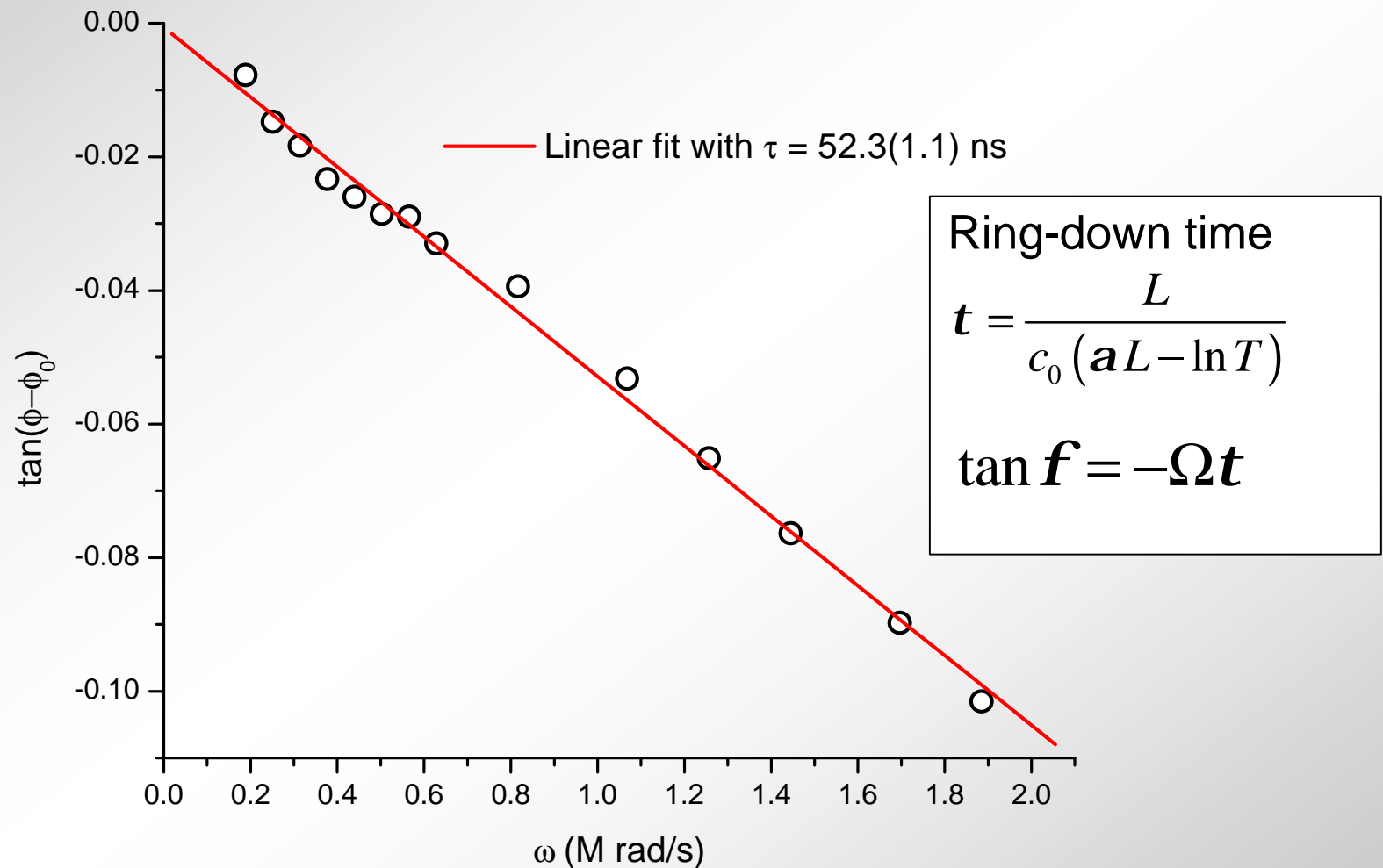
Ring-down spectroscopy on microsphere resonators



- Eroded fibre gives good coupling (very easy to break, though!)
- Tapered fibre just as good and more robust

Ring-down spectroscopy on microsphere resonators

Phase angle gives ring-down time with 5% (1 ns) accuracy



● Ring-down times correspond to Q-factor of 10^6 - 10^7

● " T " = 0.9999

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An absorption spectroscopic technique for very small samples

2. Fibre-cavity ring-down spectroscopy:

How to extract two independent (and short!) decay constants using phase-shift ring-down

3. Ring-down spectroscopy on microsphere resonators:

Measurements of absorption and refractive index

**Ring-down spectroscopy
with telecom lasers and waveguides
can be useful in chemical detection**

**Fast
Cheap
Simple
Sensitive
Compact**

Acknowledgements

Brown Group

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Dr. Albert Yang (photoacoustics)

Nick Trefiak (FLRDS)

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